

33 Reissner–Nordström Vectors

Displacement may be represented as a vector. Two types of displacement are “length scale” and “incremental distance”. Vectors representing each type act upon a common point. Ratios of components of each type may be related. Assume that the common point has vibration. Relating components will give the Reissner-Nordström metric.

Displacement Vectors;

Two 4D vectors of displacement share a common origin. One vector ($\mathbf{r}$) represents “length scale” and the other vector ($\mathbf{R}$) represents “incremental distance”. The vectors are defined as;

$$\mathbf{r} = r_1 \mathbf{e}_{11} + r_2 \mathbf{e}_{12} + r_3 \mathbf{e}_{13} + r_4 \mathbf{e}_{14}$$

$$\mathbf{R} = \partial R_1 \mathbf{e}_{21} + \partial R_2 \mathbf{e}_{22} + \partial R_3 \mathbf{e}_{23} + \partial R_4 \mathbf{e}_{24}$$

Where; $\mathbf{e}_{n1}, \mathbf{e}_{n2}, \mathbf{e}_{n3}, \mathbf{e}_{n4}$ are directional vectors (unit vectors) in 4D

(each vector has a unique frame of reference)

r_1, r_2, r_3, r_4 are components of length

$\partial R_1, \partial R_2, \partial R_3, \partial R_4$ are components of incremental displacement

The vectors have magnitude; $|\mathbf{r}| = r_5$

$$|\mathbf{R}| = \partial R_5$$

The components are related to magnitudes; $r_1^2 + r_2^2 + r_3^2 + r_4^2 = r_5^2$

$$\partial R_1^2 + \partial R_2^2 + \partial R_3^2 + \partial R_4^2 = \partial R_5^2$$

Sub-components (r_6, r_7, r_8) and ($\partial R_6, \partial R_7, \partial R_8$) are related as;

$$r_6^2 = r_5^2 - r_4^2 = r_7^2 + r_3^2 \quad \partial R_6^2 = \partial R_5^2 - \partial R_4^2 = \partial R_7^2 + \partial R_3^2$$

$$r_7^2 = r_6^2 - r_3^2 = r_1^2 + r_2^2 \quad \partial R_7^2 = \partial R_6^2 - \partial R_3^2 = \partial R_1^2 + \partial R_2^2$$

$$r_8^2 = r_6^2 - r_1^2 = r_2^2 + r_3^2 \quad \partial R_8^2 = \partial R_6^2 - \partial R_1^2 = \partial R_2^2 + \partial R_3^2$$

The Deformation Ratio;

A massive and charged object is assumed to deform surrounding space-time by a constant ratio (D);

$$D = r_8/r_7$$

Sub-components give;

$$r_6^2 = r_8^2 + r_1^2 = r_7^2 + r_3^2$$

$$r_8^2 = r_7^2 - r_1^2 + r_3^2$$

Giving; $D^2 = r_8^2/r_7^2 = 1 - r_1^2/r_7^2 + r_3^2/r_7^2$

The General Metric;

The general metric relates incremental components to the incremental magnitude;

$$\partial R_1^2 + \partial R_2^2 + \partial R_3^2 + \partial R_4^2 = \partial R_5^2$$

Vibration;

Assume that the object vibrates having a mean velocity of vibration (v_5); $v_5 = \partial R_5/\partial t_5$

Giving the “vibrational metric”; $\partial R_1^2 + \partial R_2^2 + \partial R_3^2 + \partial R_4^2 = v_5^2 \partial t_5^2$

Deformation;

The constant ratio of deformation (D) is related to other ratios of deformation;

$$D = \partial t_5/\partial t = v_5/c = \partial R_1/\partial \lambda = \partial R_2/\partial U_\theta = \partial R_3/\partial U_\phi$$

Where; c is the light constant

$\partial \lambda$ is incremental wave-length $(\partial \lambda \partial f = c)$

∂f is incremental wave-frequency $(\partial f = 1/\partial T)$

∂t is “incremental particle time”

∂T is “incremental wave time”

U_θ is arc length associated with angle (θ)

U_ϕ is arc length associated with angle (ϕ)

The vibrational metric is;

$$\partial R_1^2 + \partial R_2^2 + \partial R_3^2 + \partial R_4^2 = v_5^2 \partial t_5^2$$

Substituting with deformation gives the “wave-particle metric”;

$$D^2 \partial \lambda^2 + D^2 \partial U_\theta^2 + D^2 \partial U_\phi^2 + \partial R_4^2 = (D^2 c^2)(D^2 \partial t^2)$$

$$c^2 \partial T^2 + \partial U_\theta^2 + \partial U_\phi^2 + \partial R_4^2/D^2 = D^2 c^2 \partial t^2$$

Arc-Length;

Two arc-lengths (U_θ , U_ϕ) are associated with angles (θ , ϕ);

$$\theta = U_\theta / r \quad \text{and;} \quad \phi = U_\phi / w$$

$$r d\theta = dU_\theta \quad \text{and;} \quad w d\phi = dU_\phi$$

Where; $w = r \sin(\theta)$ and; $z = r \cos(\theta)$

$$y = w \sin(\phi) \quad \text{and;} \quad x = w \cos(\phi)$$

$$x^2 + y^2 = w^2 \quad \text{and;} \quad w^2 + z^2 = r^2 \quad \text{and;} \quad x^2 + y^2 + z^2 = r^2$$

The wave-particle metric may be written as;

$$c^2 dT^2 + r^2 d\theta^2 + r^2 \sin^2(\theta) d\phi^2 + dR_4^2 / D^2 = D^2 c^2 dt^2$$

Dimensions;

The particle dimensions of space-time are; (x, y, z, t) or $(r, \theta, \phi, -t)$

The wave dimensions of space-time are; (x, y, z, T) or $(r, \theta, \phi, -T)$

The Reissner-Nordström Metric;

The deformation ratio is; $D^2 = r_8^2 / r_7^2 = 1 - r_1^2 / r_7^2 + r_3^2 / r_7^2$

Assume; $r_7 = r$ and; $r_3 = r_Q$ and; $r_1^2 = r r_s$

Where; r_Q is the electric length scale

r_s is the Schwarzschild radius

Giving; $D^2 = r_8^2 / r_7^2 = 1 - r_s / r + r_Q^2 / r^2$

Assume; $dR_4 = dr$

Giving the Reissner-Nordström metric; $c^2 dT^2 + r^2 d\theta^2 + r^2 \sin^2(\theta) d\phi^2 + dr^2 / D^2 = D^2 c^2 dt^2$

The Schwarzschild Metric;

If; $r_Q = 0$ Then; $D^2 = D_s^2 = 1 - r_s / r$

Giving the Schwarzschild metric; $c^2 dT^2 + r^2 d\theta^2 + r^2 \sin^2(\theta) d\phi^2 + dr^2 / D_s^2 = D_s^2 c^2 dt^2$

Conclusion;

Two types of displacement are “length scale” and “incremental distance”. Vectors representing each type act upon a common point giving the Reissner-Nordström metric.